## Lecture 23

Chemical Reaction Engineering (CRE) is the field that studies the rates and mechanisms of chemical reactions and the design of the reactors in which they take place.

# Web Lecture 23 <br> Class Lecture 19-Thursday 3/21/2013 

Multiple Reactions with Heat Effects


## Multiple Reactions with Heat Effects

PFR/PBR:

$$
\frac{d T}{d V}=\frac{U a\left(T_{a}-T\right)+\sum_{i=1}^{n}\left(-r_{i j}\right)\left(\Delta H_{R x i j}\right)}{\sum_{j=1}^{m} F_{j} C_{P j}}
$$

CSTR:

$$
\operatorname{UA}\left(\mathrm{T}_{\mathrm{a}}-\mathrm{T}\right)-\mathrm{F}_{\mathrm{A} 0} \sum_{\mathrm{j}=1}^{\mathrm{m}} \mathrm{C}_{\mathrm{Pi}} \theta_{\mathrm{i}}\left(\mathrm{~T}-\mathrm{T}_{0}\right) \sum_{\mathrm{i}=1}^{\mathrm{q}}\left(\mathrm{r}_{\mathrm{ij}}\right) \mathrm{H}_{\mathrm{Rxj}}(\mathrm{~T})=0
$$

These equations are coupled with the mole balances and rate law equations.

## Multiple Reactions with Heat Effects

## Multiple Reactions

Make sure each rate of reaction and rate law are in respect to the same species (example, A); Subscripts must agree

$$
\frac{\mathrm{dT}}{\mathrm{dV}}=\frac{\mathrm{Q}_{\mathrm{g}}-\mathrm{Q}_{\mathrm{r}}}{\sum_{\mathrm{F}_{\mathrm{i}} \mathrm{C}_{\mathrm{Pi}}}}
$$

$$
\mathrm{Q}_{\mathrm{g}}=\sum \mathrm{r}_{\mathrm{ij}} \Delta \mathrm{H}_{\mathrm{Rxij}}=\mathrm{r}_{1 \mathrm{~A}} \Delta \mathrm{H}_{\mathrm{Rx} 1 \mathrm{~A}}+\mathrm{r}_{2 \mathrm{~A}} \Delta \mathrm{H}_{\mathrm{Rx} 2 \mathrm{~A}}
$$

## Multiple Reactions with Heat Effects

Multiple Reactions

1) Mole Ballances:- every species (no conversion!)
2) Rate Laws:

- relative rates
- net rates

$$
\begin{gathered}
C_{A}=C_{T 0} \frac{F_{A}}{F_{T}} p \frac{T_{0}}{T} \\
\frac{d p}{d W}=\frac{-\alpha}{2 p} \frac{F_{T}}{F_{T 0}} \frac{T}{T_{0}}
\end{gathered}
$$

## Multiple Reactions with Heat Effects

## Multiple Reactions

## 4) Heat Effects:

$$
\begin{aligned}
& \frac{\mathrm{dT}}{\mathrm{dV}}=\frac{\mathrm{Q}_{\mathrm{g}}-\mathrm{Q}_{\mathrm{r}}}{\sum \mathrm{~F}_{\mathrm{i}} \mathrm{C}_{\mathrm{Pi}}} \\
& \mathrm{Q}_{\mathrm{g}}=\text { heat produced } \\
& \mathrm{Q}_{\mathrm{r}}=\text { heat removed } \\
& \mathrm{Q}_{\mathrm{g}}=\sum \mathrm{r}_{\mathrm{ij}} \Delta \mathrm{H}_{\mathrm{Rxij}} \\
& \mathrm{Q}_{\mathrm{r}}=\mathrm{Ua}\left(\mathrm{~T}-\mathrm{T}_{\mathrm{a}}\right)
\end{aligned}
$$

$$
\left.\mathrm{Q}_{\mathrm{g}}=\sum \mathrm{r}_{\mathrm{ij}} \Delta \mathrm{H}_{\mathrm{Rxij}} \quad \text { (must have matching } \mathrm{i}, \mathrm{j}\right)
$$

## Multiple Reactions with Heat Effects

4) Heat Effects:

$$
\begin{aligned}
& \frac{d T}{d V}=\frac{Q_{g}-Q_{r}}{\sum_{i} F_{i} C_{P i}} \\
& Q_{g}=r_{1 A} \Delta H_{R 1 A}+r_{2 A} \Delta H_{R 2 A} \\
& Q_{r}=U a\left(T-T_{a}\right) \\
& \sum F_{i} C_{P_{i}}=F_{A} C_{P A}+F_{B} C_{P B}+F_{C} C_{P C}+F_{D} C_{P D} \\
& \frac{d T_{a}}{d V}=\frac{U a\left(T-T_{a}\right)}{\dot{m}_{i} C_{\text {Pool }}}
\end{aligned}
$$

5) Parameters
$\mathrm{E}_{1}, \mathrm{E}_{2}, \mathrm{~F}_{\mathrm{A} 0}, \mathrm{Ua}, \ldots$ etc

## Multiple Reactions with Heat Effects

 4) Heat Effects:$\frac{d T}{d V}=\frac{Q_{g}-Q_{r}}{\sum F_{i} C_{P i}}$
$\Delta H_{R 11 A}=-12 \mathrm{~kJ} /($ mole of A reacted in reaction 1)
$\Delta H_{R \times 2 B}=+8 k J /($ mole of B reacted in reaction 2)
$Q_{g}=r_{1 A} \Delta H_{R \times 1 A}+r_{2 B} \Delta H_{R \times 2 B}$
Use relative rates of reaction
to get $r_{2 B}$ in terms of the rate law that is given for reaction 2 ,

$$
\begin{aligned}
& \text { e.g., (2) } 3 \mathrm{~A}+2 \mathrm{~B}-->2 \mathrm{D} \\
& \quad-\mathrm{r}_{2 \mathrm{~A}}=\mathrm{k}_{2 \mathrm{~A}} \mathrm{C}_{\mathrm{A}}^{3} C_{B}^{2} \quad \text { then } \mathrm{r}_{2 \mathrm{~B}}=\frac{2}{3} \mathrm{r}_{2 \mathrm{~A}}
\end{aligned}
$$

The complex gas phase reactions
(1) $\quad \mathrm{A}+2 \mathrm{~B} \rightarrow \mathrm{C} \quad-\mathrm{r}_{1 \mathrm{~A}}=\mathrm{k}_{1 \mathrm{~A}} \mathrm{C}_{\mathrm{A}} \mathrm{C}_{\mathrm{B}}^{2} \quad \Delta \mathrm{H}_{\mathrm{Rx} 1 \mathrm{~B}}=-15,000 \mathrm{cal} / \mathrm{mol} \mathrm{B}$
(2) $\quad \mathrm{A}+\mathrm{C} \rightarrow 2 \mathrm{D} \quad-\mathrm{r}_{2 \mathrm{C}}=\mathrm{k}_{2 \mathrm{C}} \mathrm{C}_{\mathrm{A}} \mathrm{C}_{\mathrm{C}} \quad \Delta \mathrm{H}_{\mathrm{Rx} 2 \mathrm{~A}}=-10,000 \mathrm{cal} / \mathrm{mol} \mathrm{A}$
take place in a $10 \mathrm{dm}^{3}$ PFR with a heat exchanger. Plot the temperature, concentrations, molar flow rates down the length of the reactor for the following operations. E.g., Note any maximums or minimums on your plot along with how they change for the different types of operations.
(a) Adiabatic operation
(b) Heat exchange with constant $\mathrm{T}_{\mathrm{a}}$
(c) Co current heat exchange
(d) Counter current heat exchange
(e) For parts (c) and (d), plot $\mathrm{Q}_{\mathrm{r}}$ and $\mathrm{Q}_{\mathrm{g}}$ down the length of the reactor. What do you observe?

## Additional Information

$$
\begin{array}{lr}
\mathrm{C}_{\mathrm{P}_{\mathrm{A}}}=10 \mathrm{cal} / \mathrm{mol} / \mathrm{K} & \mathrm{C}_{\mathrm{P}_{\mathrm{C}}}=30 \mathrm{cal} / \mathrm{mol} / \mathrm{K} \\
\mathrm{C}_{\mathrm{P}_{\mathrm{B}}}=10 \mathrm{cal} / \mathrm{mol} / \mathrm{K} & \mathrm{C}_{\mathrm{P}_{\mathrm{D}}}=20 \mathrm{cal} / \mathrm{mol} / \mathrm{K} \\
\mathrm{k}_{1 \mathrm{~A}}=40\left(\mathrm{dm}^{3} / \mathrm{mol}\right)^{2} / \mathrm{s} / \mathrm{K} \text { at } 300 \mathrm{~K} \text { and } \mathrm{E}_{1}=8,000 \mathrm{cal} / \mathrm{mol} \\
\mathrm{k}_{2 \mathrm{C}}=2\left(\mathrm{dm}^{3} / \mathrm{mol}\right)^{2} / \mathrm{s} / \mathrm{K} \text { at } 300 \mathrm{~K} \text { and } \mathrm{E}_{2}=12,000 \mathrm{cal} / \mathrm{mol} \\
\mathrm{C}_{\mathrm{T}_{0}}=0.2 \mathrm{~mol} / \mathrm{dm}^{3}, \quad, \mathrm{C}_{\mathrm{P}_{\mathrm{Cool}}}=1 \mathrm{cal} / \mathrm{g} / \mathrm{K}, \quad \mathrm{~m}_{\mathrm{Cool}} 20 \mathrm{~g} / \mathrm{s} \\
\mathrm{Ua}=80 \mathrm{cal} / \mathrm{dm}^{3} / \mathrm{s} / \mathrm{K}, \mathrm{~T}_{\mathrm{ao}}=325 \mathrm{~K}, \mathrm{~T}_{0}=300 \mathrm{~K} \\
\mathrm{~F}_{\mathrm{A} 0}=5 \mathrm{~mol} / \mathrm{s}, \mathrm{~F}_{\mathrm{B} 0}=10 \mathrm{~mol} / \mathrm{s}, \mathrm{~F}_{\mathrm{C} 0}=0, \mathrm{~F}_{\mathrm{D} 0}=0
\end{array}
$$

POLYMATH Report

|  | Variable | Initial value | Final value |
| :---: | :---: | :---: | :---: |
| 1 | Ca | 0.0666667 | $2.49 \mathrm{E}-05$ |
| 2 | Cb | 0.1333333 | 0.0611818 |
| 3 | Cc | 0 | 0.0012689 |
| 4 | Cpa | 10. | 10. |
| 5 | Cpb | 10. | 10. |
| 6 | Cpc | 30. | 30. |
| 7 | Cpco | 10. | 10. |
| 8 | Cpd | 20. | 20. |
| 9 | Cto | 0.2 | 0.2 |
| 10 | DH1b | -1.5E+04 | -1.5E+04 |
| 11 | DH2a | -10000. | -10000. |
| 12 | E1 | 8000. | 8000. |
| 13 | E2 | 1.2E+04 | $1.2 \mathrm{E}+04$ |
| 14 | Fa | 5. | 0.0019942 |
| 15 | Fb | 10. | 4.900364 |
| 16 | Fc | 0 | 0.1016299 |
| 17 | Fd | 0 | 4.896376 |
| 18 | Ft | 15. | 9.900364 |
| 19 | k1a | 40. | 6734.733 |
| 20 | k2c | 2. | 4369.388 |
| 21 | m | 50. | 50. |
| 22 | Qg | 1422.222 | 20.21055 |
| 23 | Qr | -2000. | 1126.152 |
| 24 | R | 1.987 | 1.987 |
| 25 | r1a | -0.0474074 | -0.0006277 |
| 26 | r1b | -0.0948148 | -0.0012553 |
| 27 | r1c | 0.0474074 | 0.0006277 |
| 28 | r2a | 0 | -0.000138 |
| 29 | r2c | 0 | -0.000138 |
| 30 | r2d | 0 | 0.0002761 |
| 31 | ra | -0.0474074 | -0.0007657 |
| 32 | rb | -0.0948148 | -0.0012553 |
| 33 | rc | 0.0474074 | 0.0004896 |
| 34 | rd | 0 | 0.0002761 |
| 35 | sumFiCpi | 150. | 150. |
| 36 | T | 300. | 485.4075 |
| 37 | Ta | 325. | 471.3306 |
| 38 | Ta55 | 325. | 325. |
| 39 | To | 300. | 300. |
| 40 | Ua | 80. | 80. |
| 41 | V | 0 | 10. |
| 42 | $y$ | 1. | 1. |

## ifferential equations

$1 \mathrm{~d}(\mathrm{Fa}) / \mathrm{d}(\mathrm{V})=\mathrm{ra}$
$2 \mathrm{~d}(\mathrm{Fb}) / \mathrm{d}(\mathrm{V})=\mathrm{rb}$
$3 \mathrm{~d}(\mathrm{Fc}) / \mathrm{d}(\mathrm{V})=\mathrm{rc}$
$4 \mathrm{~d}(\mathrm{Fd}) / \mathrm{d}(\mathrm{V})=\mathrm{rd}$
$5 \mathrm{~d}(\mathrm{~T}) / \mathrm{d}(\mathrm{V})=(\mathrm{Qg}-\mathrm{Qr}) /$ sumFiCpi
$6 \mathrm{~d}(\mathrm{Ta}) / \mathrm{d}(\mathrm{V})=\mathrm{Ua} *(\mathrm{~T}-\mathrm{Ta}) / \mathrm{m} / \mathrm{Cpco}$

## Explicit equations

$1 E 2=12000$
$y=1$
$R=1.987$
$4 \mathrm{Ft}=\mathrm{Fa}+\mathrm{Fb}+\mathrm{Fc}+\mathrm{Fd}$
$5 \mathrm{To}=300$
$6 \mathrm{k} 2 \mathrm{c}=2 * \exp ((\mathrm{E} 2 / \mathrm{R}) *(1 / 300-1 / \mathrm{T}))$
$\mathrm{E} 1=8000$
Cto $=0.2$
$\mathrm{Ca}=\mathrm{Cto}{ }^{*}(\mathrm{Fa} / \mathrm{Ft})^{*}(\mathrm{To} / \mathrm{T})^{*} \mathrm{y}$
1
$10 \mathrm{Cc}=\mathrm{Cto}{ }^{*}(\mathrm{Fc} / \mathrm{Ft})^{*}(\mathrm{To} / \mathrm{T})^{*} \mathrm{y}$
11 r2c = -k2c*Ca*Cc
$12 \mathrm{Cpco}=10$
$13 \mathrm{~m}=50$
$14 \mathrm{Cb}=\mathrm{Cto}{ }^{*}(\mathrm{Fb} / \mathrm{Ft})^{*}(\mathrm{To} / \mathrm{T})^{*} \mathrm{y}$
$15 \mathrm{k} 1 \mathrm{a}=40^{*} \exp \left((\mathrm{E} 1 / \mathrm{R})^{*}(1 / 300-1 / \mathrm{T})\right)$
16 r1a $=-k 1 a^{*} C a * b^{\wedge} 2$
17 r1b = 2*r1a
$18 \mathrm{rb}=\mathrm{rlb}$
19 r2a = r2c
20 DH1b $=-15000$
21 DH2a $=-10000$
22 r1c = -r1a
$23 \mathrm{Ta} 55=325$
$24 \mathrm{Cpd}=20$
$25 \mathrm{Cpa}=10$
$26 \mathrm{Cpb}=10$
$27 \mathrm{Cpc}=30$
28 sumFiCpi $=$ Cpa*Fa + Cpb*Fb + Cpc*Fc + Cpd*Fd
$29 \mathrm{rc}=\mathrm{r} 1 \mathrm{c}+\mathrm{r} 2 \mathrm{c}$
$30 \mathrm{Ua}=80$
31 r2d $=-2 *$ r2c
32 ra = r1a+r2a
33 rd = r2d
$34 \mathrm{Qg}=\mathrm{r} 1 \mathrm{~b} * \mathrm{DH} 1 \mathrm{~b}+\mathrm{r} 2 \mathrm{a} * \mathrm{DH} 2 \mathrm{a}$
$35 \mathrm{Qr}=\mathrm{Ua*}(\mathrm{~T}-\mathrm{Ta})$




## Multiple Reactions with Heat Effects

Multiple Reactions
4) Heat Effects: $\frac{d T}{d V}=\left(-r_{A}\right)\left(-\Delta H_{R x}\right)-\frac{U a\left(T-T_{a}\right)}{\sum F_{i} C_{P i}}$

$$
\begin{aligned}
\frac{d T}{d V}=\frac{Q_{g}-Q_{r}}{\sum F_{i} C_{P i}} & Q_{g}=\text { heat produced } \\
& Q_{r}=\text { heat removed }
\end{aligned}
$$

$Q_{g}=\sum r_{i j} \Delta H_{R i j} \quad$ (must have matching $\mathrm{i}, \mathrm{j}$ )

## Multiple Reactions with Heat Effects in a PFR and CSTR

## Examples:

(1) $A+2 B \rightarrow C$
$-r_{1 A}=k_{1 A} C_{A} C_{B}^{2}$
and
$\Delta H_{R 1 A}=-20,000 \mathrm{cal} / \mathrm{mol} A$
(2) $2 A+3 C \rightarrow D$
$-r_{2 C}=k_{2 C} C_{A}^{2} C_{C}^{3}$
and
$\Delta H_{R 2 A}=10,000 \mathrm{cal} / \mathrm{mol} \mathrm{A}$

## Example A: Liquid Phase CSTR

(1) $A+2 B \rightarrow C \quad-r_{1 A}=k_{1 A} C_{A} C_{B}^{2}$

NOTE: The specific reaction rate $\mathrm{k}_{1 \mathrm{~A}}$ is defined with respect to species A.
(2) $3 C+2 A \rightarrow D \quad-r_{2 C}=k_{2 C} C_{C}^{3} C_{A}^{2}$

NOTE: The specific reaction rate $\mathrm{k}_{2 \mathrm{C}}$ is defined with respect to species C.

## Example A: Liquid Phase CSTR

The complex liquid phase reactions take place in a $2,500 \mathrm{dm}^{3}$ CSTR. The feed is equal molar in $A$ and $B$ with $\mathrm{F}_{\mathrm{A} 0}=200 \mathrm{~mol} / \mathrm{min}$, the volumetric flow rate is 100 $\mathrm{dm}^{3} / \mathrm{min}$ and the reation volume is $50 \mathrm{dm}^{3}$.

Find the concentrations of $A, B, C$ and $D$ existing in the reactor along with the existing selectivity.

Plot $F_{A}, F_{B}, F_{C}, F_{D}$ and $S_{C / D}$ as a function of $V$

## Example A: Liquid Phase CSTR

 SolutionLiquid Phase CSTR

1) Mole Balances:
(1)

$$
f\left(C_{A}\right)=v_{0} C_{A 0}-v_{0} C_{A}+r_{A} V
$$

(2)

$$
f\left(C_{B}\right)=v_{0} C_{B 0}-v_{0} C_{B}+r_{B} V
$$

(3)
$f\left(C_{C}\right)=-v_{0} C_{C}+r_{C} V$
(4)

$$
f\left(C_{D}\right)=-v_{0} C_{D}+r_{D} V
$$

2) Net Rates:

## Example A: Liquid Phase CSTR

 3) Stoichiometry:(16)

$$
\mathrm{C}_{\mathrm{A}}=\mathrm{F}_{\mathrm{A}} / \mathrm{v}_{0}
$$

(17)

$$
C_{B}=F_{B} / v_{0}
$$

(18)

$$
\mathrm{C}_{\mathrm{C}}=\mathrm{F}_{\mathrm{C}} / v_{0}
$$

(19)

$$
\mathrm{C}_{\mathrm{D}}=\mathrm{F}_{\mathrm{D}} / v_{0}
$$

4) Parameters:
(20) $v_{0}=100 \mathrm{dm}^{3} / \mathrm{min}$
(21) $\mathrm{k}_{1 \mathrm{~A}}=10\left(\mathrm{dm}^{3} / \mathrm{mol}\right)^{2} / \mathrm{min}$
(22) $\quad \mathrm{k}_{2 \mathrm{C}}=15\left(\mathrm{dm}^{3} / \mathrm{mol}\right)^{4} / \mathrm{min}$

## Example B: Liquid Phase PFR

Takes place in a PFR. The feed is equal molar in A and $B$ and $F_{A 0}=200 \mathrm{~mol} / \mathrm{min}$ and the volumetric flow rate is $100 \mathrm{dm}^{3} / \mathrm{min}$. The reaction volume is $50 \mathrm{dm}^{3}$ and the rate constants are:
$k_{1 A}=10\left(\mathrm{dm}^{3} / \mathrm{mol}\right)^{2} / \mathrm{min}$
$k_{2 C}=15\left(\mathrm{dm}^{3} / \mathrm{mol}\right)^{4} / \mathrm{min}$
Rate laws are the same as Example A.
Plot $F_{A}, F_{B}, F_{C}, F_{D}$ and $S_{C / D}$ as a function of $V$.

## Example B: Liquid Phase PFR

1) Mole Balances:

$$
\begin{array}{lr}
\frac{d F_{A}}{d V}=r_{A} & \left(F_{A 0}=200 \mathrm{~mol} / \mathrm{min}\right) \\
\frac{d F_{B}}{d V}=r_{B} & \left(F_{B 0}=200 \mathrm{~mol} / \mathrm{min}\right) \\
\frac{d F_{C}}{d V}=r_{C} & V_{F}=50 \mathrm{dm}^{3} \\
\frac{d F_{D}}{d V}=r_{D} &
\end{array}
$$

## Example B: Liquid Phase PFR

2) Net Rates:
(5)

$$
r_{A}=r_{1 A}+r_{2 A}
$$

(6)

$$
r_{B}=r_{1 B}
$$

(7)

$$
r_{C}=r_{1 C}+r_{2 C}
$$

(8)

$$
r_{D}=r_{2 D}
$$

2) Rate Laws:
(9) $\quad r_{1 A}=-k_{1 A} C_{A} C_{B}^{2}$

22
(10)

$$
r_{2 C}=-k_{2 C} C_{A}^{2} C_{C}^{3}
$$

## Example B: Liquid Phase PFR

2) Relative Rates:

$$
\frac{r_{1 A}}{-1}=\frac{r_{1 B}}{-2}=\frac{r_{1 C}}{1} \quad \text { Reaction } 1
$$

(11) $r_{1 B}=2 r_{1 A}$
(12) $\quad r_{1 C}=-r_{1 A} \quad$ Reaction 2

$$
\frac{r_{2 A}}{-2}=\frac{r_{2 C}}{-3}=\frac{r_{2 D}}{1}
$$

(13) $\quad r_{2 A}=2 / 3 r_{2 C}$
(14) $\quad r_{2 D}=-1 / 3 r_{2 C}$

## Example B: Liquid Phase PFR

## 2) Rate Laws:

$$
\begin{array}{ll}
r_{1 A}=-k_{1 A} C_{A} C_{B}^{2} & (5) \\
k_{1 A}=k_{1 A 1} \exp \left[\left(E_{1} / R\right)\left(1 / T_{1}-1 / T\right)\right](6) \\
r_{2 C}=-k_{2 C} C_{A}^{2} C_{C}^{3} & \text { (7) } \\
r_{2 C}=k_{2 C 2} \exp \left[\left(E_{2} / R\right)\left(1 / T_{2}-1 / T\right)\right](8) \\
r_{A}=r_{1 A}+r_{2 B} & \text { (9) } r_{B}=r_{1 B}(10) \\
r_{C}=r_{1 C}+r_{2 C} & (11) r_{D}=r_{2 D}(12) \\
r_{1 C}=-r_{1 A} & (13) r_{1 B}=2 r_{1 A}(13) \\
r_{2 A}=2 / 3 r_{2 C} & (15) r_{2 D}=-1 / 3 r_{2 C}(16)
\end{array}
$$

## Example B: Liquid Phase PFR

3) Stoichiometry:

$$
\begin{array}{lll}
C_{A}=C_{T 0} \frac{F_{A}}{F_{T}} p \frac{T_{0}}{T} & (17) & C_{B}=C_{T 0} \frac{F_{B}}{F_{T}} p \frac{T_{0}}{T} \\
C_{C}=C_{T 0} \frac{F_{C}}{F_{T}} p \frac{T_{0}}{T} & (19) & C_{D}=C_{T 0} \frac{F_{D}}{F_{T}} p \frac{T_{0}}{T} \\
F_{T}=F_{A}+F_{B}+F_{C}+F_{D} & (21) & \frac{d p}{d V}=\frac{-\alpha \rho}{2 p} \frac{F_{T}}{F_{T 0}} \frac{T}{T_{0}}
\end{array}
$$

## Multiple Reactions with Heat Effects

4) Heat Effects:

$$
\begin{align*}
& \frac{d T}{d V}=\frac{Q_{g}-Q_{r}}{\sum_{F} F_{P i}}  \tag{23}\\
& \frac{d T_{a}}{d V}=\frac{U a\left(T-T_{a}\right)}{\dot{m}_{i} C_{P c o o l}} \\
& Q_{g}=r_{1 A} \Delta H_{R 1 A}+r_{2 A} \Delta H_{R 2 A}  \tag{24}\\
& Q_{r}=U a\left(T-T_{a}\right)  \tag{25}\\
& \sum C_{P}=F_{A} C_{P A}+F_{B} C_{P B}+F_{C} C_{P C}+F_{D} C_{P D} \tag{27}
\end{align*}
$$

Parameters:

$$
E_{1}, E_{2}, F_{A 0}, \ldots
$$

## Selectivity

If one were to write $S_{C / D}=F_{C} / F_{D}$ in the Polymath program, Polymath would not execute because at $\mathrm{V}=0$, $\mathrm{F}_{\mathrm{C}}=0$ resulting in an undefined volume (infinity) at $\mathrm{V}=0$. To get around this problem we start the calculation $10^{-4}$ $\mathrm{dm}^{3}$ from the reactor entrance where $F_{D}$ will not be zero and use the following IF statement.
(15) $\quad S_{C / D}=$ if $(V>0.001)$ then $\left(\frac{F_{C}}{F_{D}}\right)$ else (0)

## Selectivity

3) Stoichiometry:
(16)

$$
\mathrm{C}_{\mathrm{A}}=\mathrm{F}_{\mathrm{A}} / v_{0}
$$

(17)

$$
\mathrm{C}_{\mathrm{B}}=\mathrm{F}_{\mathrm{B}} / v_{0}
$$

(18)

$$
\mathrm{C}_{\mathrm{C}}=\mathrm{F}_{\mathrm{C}} / v_{0}
$$

(19)

$$
\mathrm{C}_{\mathrm{D}}=\mathrm{F}_{\mathrm{D}} / \mathrm{v}_{0}
$$

## Parameters:

(20)
$v_{0}=100 \mathrm{dm}^{3} / \mathrm{min}$
(21) $\mathrm{k}_{1 \mathrm{~A}}=10\left(\mathrm{dm}^{3} / \mathrm{mol}\right)^{2} / \mathrm{min}$
(22) $\quad \mathrm{k}_{2 \mathrm{C}}=15\left(\mathrm{dm}^{3} / \mathrm{mol}^{4} / \mathrm{min}\right.$

## End of Web Lecture 23 <br> Class Lecture 18

